



Analysis of Series RC Circuits in Signal Processing

Adhyayan kumar, UG Student, Dept. of ECE, GIET University,
23ece051.adhyayankumar@giet.edu

Pritam kumar Ghia, UG Student, Dept. of ECE, GIET University,
23ece074.pritamkumarghia@giet.edu

Aadersh Gupta, UG Student, Dept. of ECE, GIET University,
23ece066.aadershkumargupta@giet.edu

Binaya kumar Bastia, UG Student, Dept. of ECE, GIET University,
23ece057.binayakumarbastia@giet.edu

Abstract: A Series RC Circuit, comprising a resistor (R) and capacitor (C) in series, exhibits complex impedance characteristics influenced by the RC time constant, which determines the circuit's response rate. The voltage and current dynamics of the circuit are governed by charge accumulation and current decay over time. Impedance varies with frequency, enabling the circuit to filter signals for advanced signal processing. With a specific cut-off frequency and phase shift, the circuit is useful in applications such as low-pass and high-pass filtering, oscillators, and timing circuits, as well as in audio, video, medical, communication, and power systems. Analytical methods for RC circuits involve impedance, voltage, current, and power calculations, often using Kirchoff's laws, circuit theorems, and Laplace transforms. Understanding Series RC Circuits is crucial for designing and analysing electronic systems, ensuring optimized signal processing, power management, and circuit stability. Their simplicity and versatility make them fundamental in both basic and advanced electronic systems.

Keywords--- Series RC Circuit, RC time constant, impedance, filtering, signal processing, circuit analysis.

1. Introduction:

The series RC circuit, composed of a resistor (R) and capacitor (C) connected in series, is a cornerstone of electronic design, known for its essential role in controlling and manipulating electrical signals. At the heart of its operation lies the RC time constant, ($\tau = RC$), which defines the circuit's dynamic response by determining the rate at which the capacitor charges and discharges [1]. This time constant not only dictates the speed of response but also underpins the frequency-dependent behaviour of the RC circuit, making it invaluable in signal processing applications. The voltage response across the capacitor, expressed as $V_C(t) = V_0(1 - e^{-t/RC})$, reveals how the capacitor accumulates charge over time, showing a characteristic exponential increase [2]. Concurrently, the current, defined by $I(t) = V_0/R(e^{-t/RC})$, exhibits an exponential decay as the circuit stabilizes, which further illustrates the smooth, time-dependent adjustment intrinsic to RC circuits [2]. The impedance of this circuit, given by $Z = R + \frac{1}{j\omega C}$, is complex and frequency-dependent, allowing the circuit to selectively permit or impede different frequency components [3]. This property establishes the RC circuit as a versatile tool for applications in filtering, where it functions to isolate desired frequency bands from unwanted ones [4]. At a deeper level, the RC circuit's behaviour can be precisely tuned for various applications through its cut-off frequency, ($f_c = \frac{1}{2\pi RC}$), which serves as a threshold frequency for attenuating or passing signals [4]. The circuit's phase shift, $\phi = \tan^{-1}(\frac{1}{j\omega C})$, introduces a phase delay between voltage and current, a critical factor in timing and synchronization [5].



This frequency-dependent phase shift and amplitude response are fundamental to many signal-processing and timing-based applications, providing the underlying architecture for oscillators, waveform shaping, and filtering [6].

The versatility and simplicity of the RC circuit make it an essential component across a broad spectrum of electronic systems [7]. Its implementation ranges from low-pass and high-pass filtering in audio and video devices to critical roles in timing circuits, medical devices, and control systems [6]. As such, a comprehensive understanding of the RC circuit's characteristics and behaviour is fundamental to advancing applications in electronics, communications, and biomedical technology [8]. This research examines the frequency-dependent properties of the RC circuit, with a focus on its impedance, phase shift, and filtering capabilities, and explores its applications across diverse fields [1]. Here, in this article, we present and discuss the graphs for different values of variable resistance and capacitors connected in series, to analyse the behaviour of series RC circuit and the range of input frequency for safe application.

2. Methodology:

This research investigates the behaviour of a Series RC Circuit, which comprises a resistor (R) and capacitor (C) connected in series. The primary focus is on the circuit's output behaviour at different values of Capacitance. We also focus on circuit's impedance characteristics, which are essential for understanding its applications in signal processing and circuit design. The RC time constant, defined as $\tau = RC$, is a critical parameter that influences the circuit's transient behaviour and overall response to voltage and current inputs. The time-domain responses of the circuit are modelled using established equations: the voltage across the capacitor is given by $V_C(t) = V_0(1 - e^{-t/RC})$, and the current through the circuit is described by $I(t) = V_0/R(e^{-t/RC})$. These equations facilitate the examination of how the capacitor charges and discharges over time, revealing insights into the circuit's dynamic behaviour. To explore the frequency-dependent characteristics of the Series RC Circuit, we compute the impedance, represented as $Z = R + \frac{1}{j\omega C}$. This expression allows for the analysis of how the circuit responds to different frequencies, emphasizing its role in filtering applications. The cut-off frequency, $f_c = \frac{1}{2\pi RC}$, is derived from the impedance analysis, marking the threshold at which the circuit begins to attenuate high-frequency signals. The phase shift ϕ is determined using $\phi = \tan^{-1}(\frac{1}{j\omega C})$, providing insight into the timing relationship between voltage and current. Practical implementations of the Series RC Circuit are examined to highlight its applications in low-pass and high-pass filtering, oscillators, and timing circuits. Each application is explored through specific circuit configurations and the resulting impact on signal integrity and processing capabilities. Additionally, the methodology includes evaluating the power dissipation across the components to ensure efficiency in both signal processing and power management. The analysis employs Kirchhoff's laws to derive equations governing the circuit, alongside circuit theorems such as Thevenin's and Norton's theorems, to simplify complex circuits into manageable components. The Laplace transform is utilized to analyse circuit behaviour in the



frequency domain, facilitating a deeper understanding of transient and steady-state responses. This comprehensive methodology not only lays the foundation for the design and analysis of electronic systems but also underscores the Series RC Circuit's significance as a fundamental building block in various applications. By examining both theoretical and practical aspects, this research aims to enhance the understanding of RC circuits and their diverse applications in modern electronics, from simple filters to complex communication systems.

3. Result and Discussion:

A series R-C circuit plays a versatile role in electronics, functioning as a filter, signal processor, and frequency selector. It allows precise filtering, including low-pass, high-pass, band-pass, and band-stop, enabling control over which frequencies pass through or are attenuated. By filtering unwanted frequencies, it enhances signal clarity and minimizes interference. Additionally, the r-c circuit is useful in signal coupling, helping to pass desired signals from one stage to another while maintaining integrity. Its impedance-matching capabilities ensure efficient energy transfer between circuit elements, improving performance, while attenuation adjusts signal levels to suit different stages within a circuit.

Through resonance, the circuit allows for frequency selection, targeting specific frequencies while rejecting others, which is essential in radio tuning and other signal-processing applications. Beyond frequency control, the circuit provides critical overvoltage, transient, and noise protection. This helps shield sensitive electronic components from potential damage due to sudden voltage spikes or external electromagnetic interference, ensuring circuit stability. Moreover, an r-c circuit assists in waveform shaping by altering the shape of input signals, such as converting a square wave to a more rounded form. It can also promote oscillation, forming the basis for oscillators in generating steady signals. Its multifunctional design makes it essential in analog signal processing and control.

Here we have used Proteus software as a tool to simulate the RC Series circuit design and its output behaviour. In our initial design, we constructed a Series RC circuit incorporating a resistor with a value of $1\text{ k}\Omega$ and a capacitor with a capacitance of $100\text{ }\mu\text{F}$. This configuration was connected to an AC source providing a 10 V output voltage at a frequency of 1 Hz . To observe the circuit's behaviour, a virtual digital oscilloscope was connected, with Channel 1 (A) monitoring the input voltage, Channel 2 (B) linked to the output terminal of the capacitor, and Channel 3 (C) grounded. Additionally, a green LED was connected in parallel with the capacitor, allowing us to visually monitor the capacitor's charging and discharging cycles. This setup enabled detailed analysis of the voltage across the capacitor in response to the AC input, providing insight into the circuit's time-dependent behaviour and the role of capacitance in an AC environment. Output is observed and plotted, Yellow line represents Input Voltage and Blue line represents output voltage in the plot.

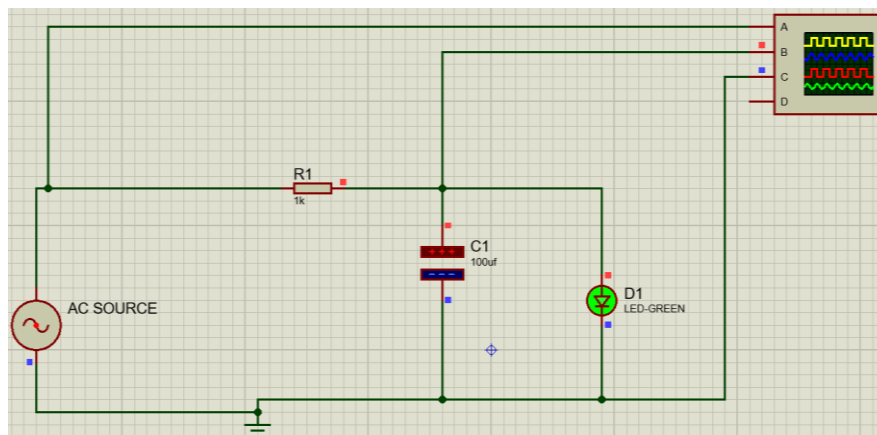


Fig. 1: This diagram demonstrates the circuit diagram of single-phase ac circuit with a resistance and capacitance in series, and a green led connected in parallel with capacitor.

Components required: Resistor(1k), Capacitor (100 μ F), Voltage source (AC), DSO.
 Following sequence have been followed for getting results from the designed RC circuit:

1. Create a virtual simulation software project
2. Placed the components like resistor, capacitor etc from the software library
3. Connected the wires with components in series
4. Assign the values to the components
5. Simulate the circuit
6. Analyse and view the simulation using the DSO tools
7. Change values of the component for different outputs

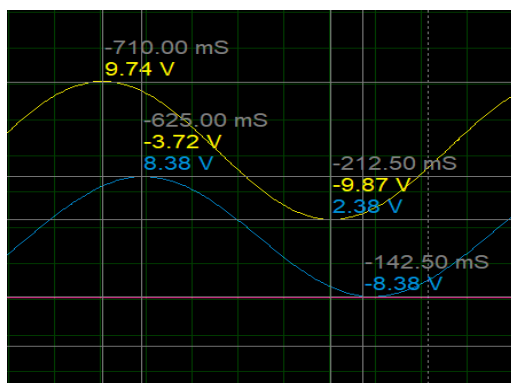


Fig. 2: R=1 k Ω , C= 100 μ F input (9.87 V), output (8.38 V)

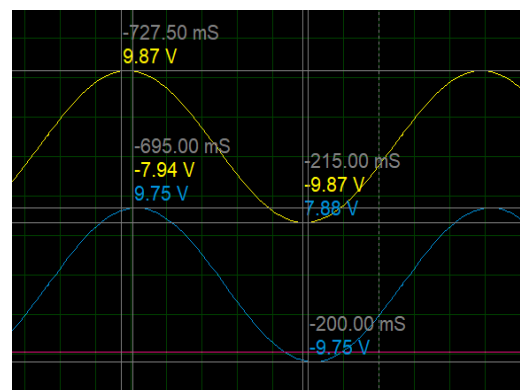


Fig. 3: R=0.5 k Ω , C= 100 μ F input (9.87 V), output (9.75 V)

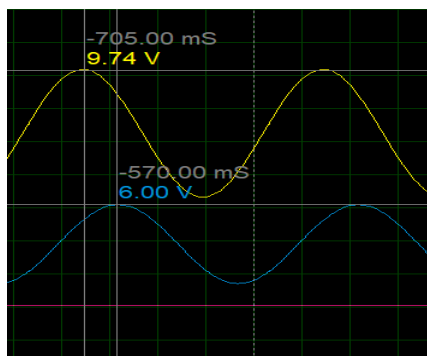


Fig 4: R=1 kΩ, C = 200 μF input (9.87), output (6.00)

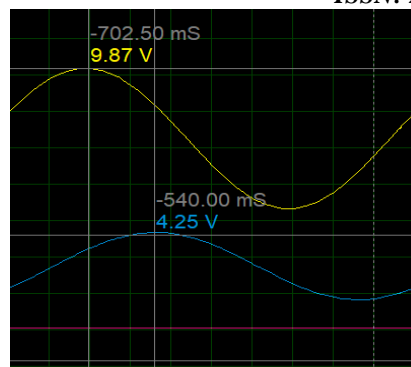


Fig 5: R=2 kΩ, C= 100 μF input (9.87), output (4.25)

4. Outcomes:

According to the Simulated graphs we have tabulated the values in the below table:

Table 1: Comparison of Parameters

Resistance (kΩ)	Capacitance (μF)	Frequency (Hz)	Input Voltage (V)	Output Voltage (theoretical)	Output Voltage (practical)
0.5	100	1	9.87	9.41	9.75
0.5	200	1	9.87	8.01	8.00
1	100	1	9.87	8.35	8.37
1	200	1	9.87	6.14	6.00
2	100	1	9.87	4.25	4.25
2	200	1	9.87	3.63	3.63

The observed output amplitudes (in volts) across the capacitor demonstrated a decreasing trend as a function of the input capacitance value, while keeping the resistance and input frequency constant. This inverse relationship highlights how increasing capacitance affects the voltage across the capacitor in an RC circuit under AC conditions. Specifically, as capacitance increases, the capacitive reactance decreases, resulting in lower output amplitude across the capacitor for a given input voltage and frequency. This behaviour underscores the sensitivity of output voltage to capacitance in RC circuits, reinforcing the importance of precise capacitance selection for applications requiring specific output characteristics.

The relationship between input frequency and output voltage is $\{\text{Input frequency} \propto \frac{1}{\text{output voltage}}\}$. In systems where frequency conversion is applied, as the input frequency increases, the output voltage tends to decrease, assuming other variables are held constant. This inverse proportionality often comes into play in frequency-sensitive circuits where maintaining a stable output voltage is crucial. Such a relationship is vital in applications involving filters and resonators, where controlling the output voltage by adjusting the input frequency allows for finer tuning and more efficient energy management.



Dependency of Output Frequency on Capacitance Rating: In various electronic and electrical circuits, the output frequency is directly influenced by the capacitance value used within the system. Higher capacitance values typically result in lower output frequencies, as capacitors take longer to charge and discharge. This dependency is particularly important in oscillators and filters, where capacitors are used to determine the cutoff frequencies or oscillation rates. As a result, the choice of capacitance rating must be carefully selected to achieve the desired output frequency for stable and predictable circuit performance.

The capacitance value in a system is inversely proportional to its pass capacity

$$\{ \text{Capacitance value} \propto \frac{1}{\text{pass capacity}} \},$$

meaning that as capacitance increases, the pass capacity (or the ability to pass certain frequencies) decreases. This relationship plays a crucial role in filter circuits, where capacitors are used to either allow or block specific frequency ranges. In essence, a higher capacitance value restricts the passage of higher frequencies, making it a central component in tuning and filtering applications. By manipulating capacitance values, engineers can design circuits that target specific frequencies, improving system efficiency and ensuring precise control over signal transmission. So according to the outcomes gained from the simulated graphs and table we can see the RC series circuit behaves like a Low pass Filter. To prove we use formulas and equations of Frequency response of Low Pass Filter.

In Laplace domain;

$$\text{Resistance} = R$$

$$\text{Capacitive Reactance } X_c = \frac{1}{sC}$$

$$V_{(out)} = V_{(in)} \times \frac{\frac{1}{sC}}{R + \frac{1}{sC}}$$

$$\frac{V_{out}}{V_{in}} = \frac{1}{RCs + 1}$$

$$\left| \frac{V_{out}}{V_{in}} \right| = \frac{1}{\sqrt{(RC\omega)^2 + 1}} \text{ since } \{s = j\omega, 1 + j\omega RC\}$$

According to the calculations we have plotted the graph which show the behaviour of RC Series circuit as a Low pass filter.

When we put the values to our calculations, we get the following output at 1 Hz frequency:

$$\left| \frac{V_{out}}{V_{in}} \right| = \frac{1}{\sqrt{(1 \times 25 \times 10^{-6} \times 6.28)^2 + 1}} = 0.988$$

Here, $R = 1 \text{ k}\Omega$, $C = 25 \text{ }\mu\text{F} = 25 \times 10^{-6}$, $\omega = 2 \times \pi \times f = 6.28$

5. Graphical representation:

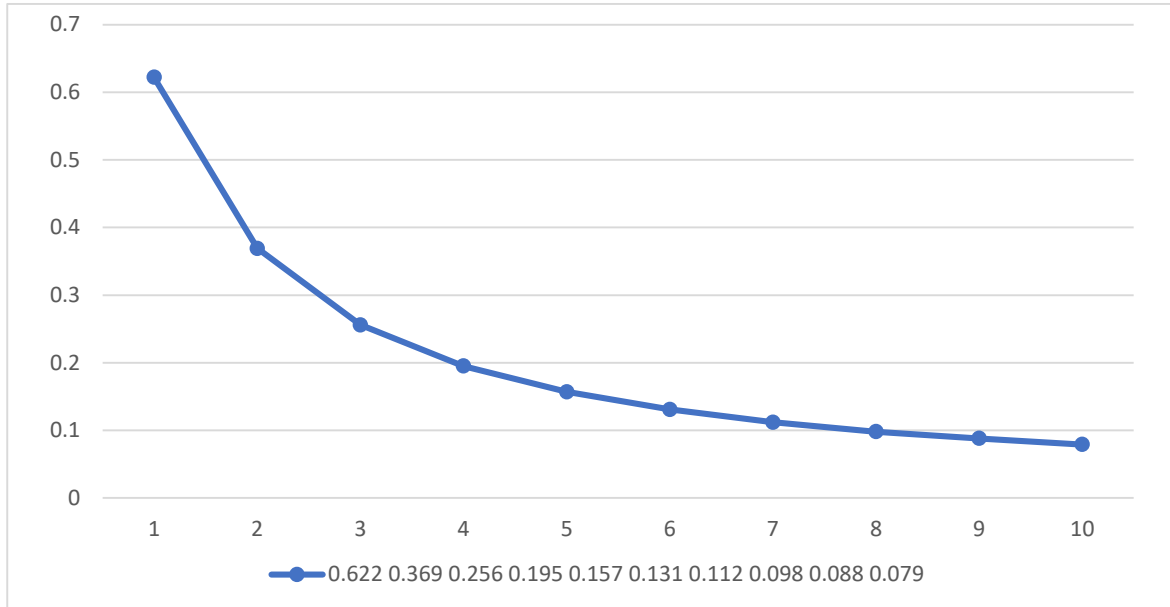


Fig 6: Frequency vs Gain (at 2 kΩ,100 μF)

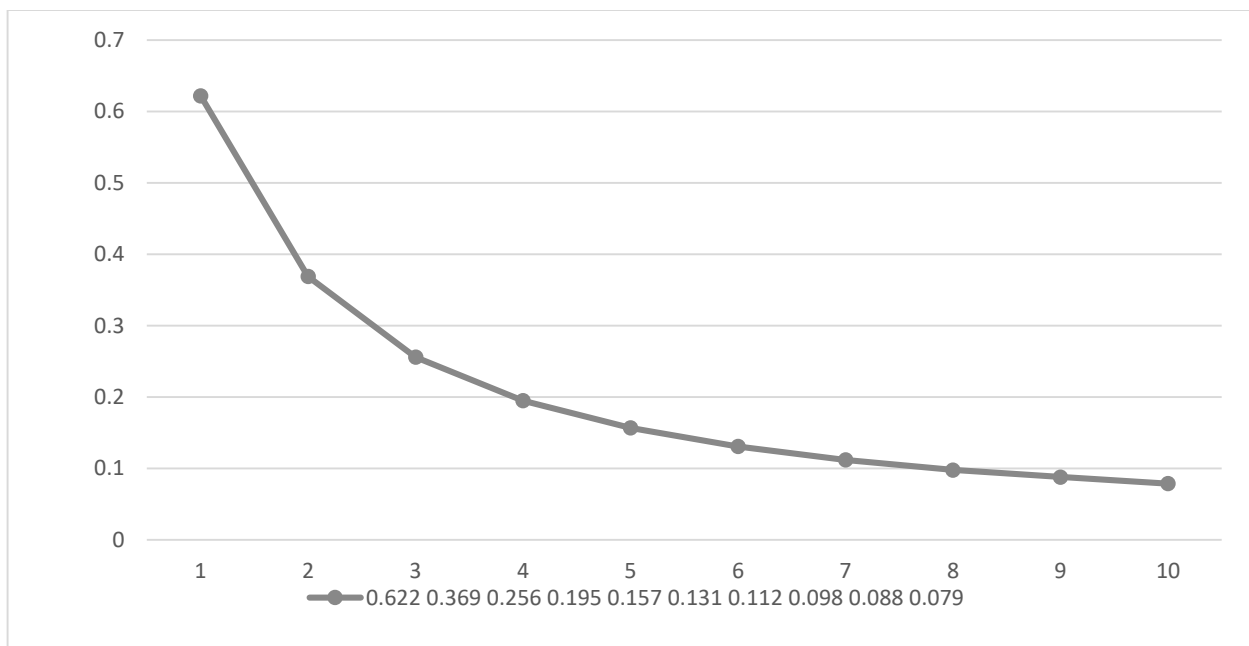


Fig 7: Frequency vs Gain (at 1 kΩ,100 μF)

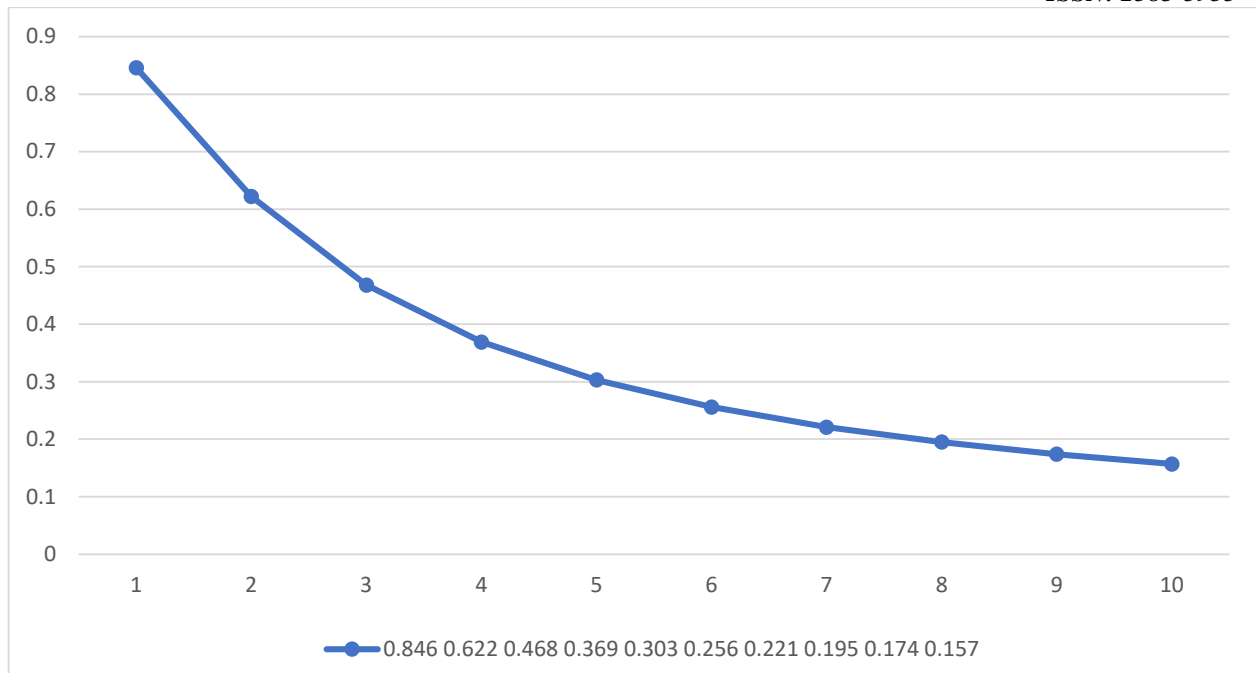


Fig 8: Frequency vs Gain

From the calculated values, we plotted a graph which represents an exponential decrease of gain with respect to frequency

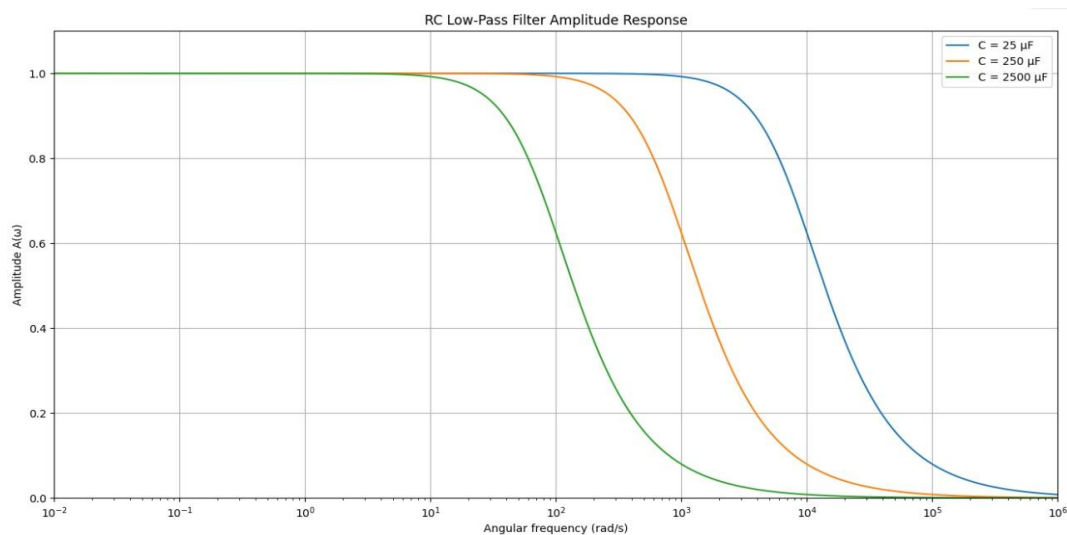


Fig 9: Graphical representation of low pass filter

6. Conclusion

This research paper has explored the dynamics of Series RC Circuits, highlighting their essential role in electronic systems through an analysis of impedance characteristics governed by the RC time constant. By examining the voltage and current responses, along with impedance calculations, we gained a comprehensive understanding of the circuit's behaviour



under varying conditions. Key findings show that Series RC Circuits enable low-pass and high-pass filtering, serving as crucial components in applications like oscillators, timing circuits, and signal coupling. The established cutoff frequency and phase shift provide insights into the circuit's filtering capabilities and timing relationships. Practical implementations further emphasize the circuit's versatility, proving vital for efficient signal processing, power management, and circuit stability. Employing Kirchhoff's laws, circuit theorems, and the Laplace transform enabled a thorough analysis of both transient and steady-state responses, establishing the Series RC Circuit as a foundational component in various electronic applications. In conclusion, this study underscores the significance of Series RC Circuits in modern electronics, revealing their broad range of applications and potential for innovation, with continued exploration promising to enhance their functionality and integration into complex communication system.

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